## High Marginal Tax Rates on the Top 1\%?

Lessons from a Life Cycle Model with Idiosyncratic Income Risk

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## Motivation: Income Share of Top $1 \%$ in the U.S.

Top 1 Percent Income Share in the United States


Source: Source is Piketty and Saez (2003) and the World Top Incomes Database.

## Motivation: Top Marginal Income Tax Rates

Top Marginal Income Tax Rates, 1900-2011


Source: Piketty and Saez (2013, figure 1).

## Motivation

- Large secular increase in earnings, income and wealth inequality: increasing share of the "Top 1\%"
- Popular and scientific calls for increasing marginal tax rates at the top, e.g. Diamond and Saez (2011), Reich (2010), Piketty (2014)


## Motivation

- Large secular increase in earnings, income and wealth inequality: increasing share of the "Top 1\%"
- Popular and scientific calls for increasing marginal tax rates at the top, e.g. Diamond and Saez (2011), Reich (2010), Piketty (2014)
- Scientific basis: Diamond/Saez (2011): Revenue maximizing top marginal tax rate above fixed income threshold $\bar{y}$ :

$$
\tau_{h}=\frac{1}{1+a \cdot \epsilon}
$$

- $a=\frac{1}{1-1 /\left(y_{m} / \bar{y}\right)}$ measures thickness of tail of income distribution
- $\epsilon$ : Average elasticity of earnings (in top bracket) w.r.t. net of tax rate $\epsilon=\frac{d \log (y)}{d \log (1-\tau)}$
- Generalization to dynamic models: Badel and Huggett (2016)
- Diamond/Saez estimates: $a=1.5$ and $\epsilon=0.25$
$\rightarrow \tau_{h}=0.73$ maximizes tax revenue from top $1 \%$ earnings
- More on the Formula


## Details of the Formula (relevant for this paper)

- Static model of labor supply. Labor productivity e distributed Pareto with tail parameter $a_{e}$ in population.
- Constant marginal tax rate $\tau$ above threshold $\bar{y}$. Discard revenue.
- Peak of the Laffer curve if $\bar{y}$ is held fixed (alternatively, if share of population subject to top marginal rate -say top $1 \%$ - fixed):

$$
\tau_{h}=\frac{1}{1+a \cdot \epsilon} \quad \text { and } \quad \tau_{h}^{1 \%}=\frac{1}{1+\epsilon}
$$

where

$$
\epsilon=\frac{1}{a} \cdot \epsilon_{u}+\left[1-\frac{1}{a}\right] \cdot \epsilon_{c}
$$

- Assume preferences given by

$$
U(c, n)=\frac{c^{1-\gamma}}{1-\gamma}-\lambda \frac{n^{1+1 / \chi}}{1+1 / \chi}
$$

## Details of the Formula (continued)

- Suppose $\gamma=0$ : No income effects. Then $\epsilon_{u}=\epsilon_{c}=\chi, a=\frac{a_{e}}{1+\chi}$ and

$$
\tau_{h}=\frac{1}{1+a \cdot \chi} \quad \text { and } \quad \tau_{h}^{1 \%}=\frac{1}{1+\chi}
$$

- With income effects $(\gamma>0)$ : Then $\epsilon_{u}=\frac{1-\gamma}{\gamma+1 / \chi}, \epsilon_{c}=\frac{1}{\gamma+1 / \chi}$ and

$$
\tau_{h}=\tau_{h}\left(\chi, \gamma, a_{e}\right) \quad \text { and } \quad \tau_{h}^{1 \%}=\tau_{h}^{1 \%}\left(\chi, \gamma, a_{e}\right)
$$

- Basic upshots:
- Exact tax experiment important: $\tau_{h}$ vs $\tau_{h}^{1 \%}$.
- (Obviously) Frisch labor supply elasticity $\chi$ important.
- Size of the income effect (parameterized by $\gamma$ ) important.
- Labor productivity process $e$ at the top (through $a_{e}$ ) important.


## Objective of this project

- Evaluate Diamond/Piketty/Saez recommendations in a (relatively standard) heterogeneous households macro model
- Key ingredients of the analysis:
- Life cycle model with endogenous labor supply, savings decisions
- Incomplete markets and general equilibrium
- Ex ante and ex post heterogeneity: Redistribution vs. Insurance
- Progressive tax schedule that adjusts to changes in $\tau_{h}$
- Maximization over tax-reform-induced transition paths:


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- Progressive tax schedule that adjusts to changes in $\tau_{h}$
- Maximization over tax-reform-induced transition paths:
- Evolution of wealth distribution and factor prices over time
- Welfare impact on transitional generations
- Key challenge: How to generate realistic earnings and wealth distribution at the top $1 \%$ ?
$\rightarrow$ We use rare but large labor productivity shocks not observed in survey data (Castaneda/Diaz-Gimenez/Rios-Rull, 2003)


## Central Result I: Revenue Maximization

- Peak of Laffer curve from top $1 \%$ earners is at higher marginal tax rates $\left(\tau_{h}=87 \%\right)$ than advocated by Diamond and Saez.
- Intuition:
- Productivity realizations at the very top large, persistent (but not permanent)
- Given calibrated preferences, individuals at the very top of productivity distribution maintain labor supply even at very high marginal tax rates
$\Rightarrow$ Uncompensated elasticity of earnings w.r.t. tax rate is low at the top (strong income effects).


## Central Result II: Welfare Maximization

- Revenue maximizing $\tau_{h}=87 \%$ rate is not welfare maximizing, but not that far off. Social welfare maximized at $\tau_{h}=79 \%$.
- Intuition: High tax progressivity
- is detrimental for macro aggregates
- lower capital stock
- lower wages
- hurts the top $1 \%$ who receive weight in social welfare function
- but provides social insurance against never making it into Top $1 \%$.


## The Model: Overview

- Large-scale OLG model as in Auerbach and Kotlikoff (1987)
- Neoclassical production sector
- Life cycle structure with population growth, retirement age $j_{r}$, uncertain survival, terminal age $J$
- Consumption-savings, labor supply decisions s.t. idiosyncratic wage risk (Bewley, Huggett, Aiyagari, Imrohoroglu, Kaplan and Violante)
- Wage is given by $e(j, s, \alpha, \eta) w$
- Preferences

$$
U(c, n)=\frac{c^{1-\gamma}}{1-\gamma}-\lambda \frac{n^{1+1 / \chi}}{1+1 / \chi}
$$

- Benevolent government (values transitional generations)
- Chooses optimal (within parametric class) progressive labor income tax reform $\tau_{h}, \tau_{l}$ and required time path of government debt $B_{t}$.
- Takes other elements of fiscal policy as fixed $\tau_{c}, \tau_{k}, \tau_{s s}$.


## The Model

Households: Labor productivity

- Households are ex ante and ex post heterogeneous w.r.t. labor productivity
- Wage is given by $w \cdot e(j, s, \alpha, \eta)$ :
- Wage rate of the economy $w$
- Deterministic education level $s \in\{n, c\}$ determined at birth
- Deterministic age component $\epsilon_{j, s}$
- Fixed effect $\alpha$ determined at birth
- Stochastic component $\eta$ following education specific Markov chain with states $\eta \in \mathcal{E}_{s}$ and transition matrix $\pi_{s}\left(\eta, \eta^{\prime}\right)$.


## The Model

Households: Decision making

- At each point in time households choose
- consumption $c$
- labor supply $n$ and thus earnings $y=w \cdot e \cdot n$
- savings in the risk free asset $a$ at return $r_{n}=r\left(1-\tau_{k}\right)$ and with tight borrowing constraint
- Preferences

$$
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$$

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$$
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$$

- Dynamic optimization problem:

$$
\begin{aligned}
& v(j, s, \alpha, \eta, a)=\max _{c, n, a^{\prime} \geq 0} U(c, n)+\beta \psi_{j+1} \sum_{\eta^{\prime}} \pi_{s}\left(\eta^{\prime} \mid \eta\right) v\left(j+1, s, \alpha, \eta^{\prime}, a^{\prime}\right) \\
& \left(1+\tau_{c}\right) c+a^{\prime}+T(y)+T_{s s}(y)=\left(1+r_{n}\right) a+b(j, s, \alpha, \eta)+y
\end{aligned}
$$

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\end{aligned}
$$

## The Model

Government

- Collects revenue from
- consumption taxes $\tau_{c}$
- flat capital income tax $\tau_{k}$
- progressive labor earnings tax $T(\cdot)$
- Finances exogenous expenditure stream $G$
- Chooses time path of debt $B_{t}$
- Runs a PAYG progressive social security system
- Budget constraint

$$
\begin{aligned}
& r \tau_{k} \int a^{\prime}(.) d \Phi+\tau_{c} \int c(.) d \Phi+\int T(w e(j, s, \alpha, \eta) n(.)) d \Phi \\
= & G+(r-n) B
\end{aligned}
$$

## Definition of Recursive Competitive Equilibrium

 Given $G,, B$, tax system $\left(\tau_{c}, \tau_{k}, T\right)$ and social security system $\left(\tau_{s s}, \bar{y}_{s s}\right)$, a stationary recursive competitive equilibrium is value and policy functions ( $v, c, n, a^{\prime}$ ) for the household, optimal input choices $(K, L)$ of firms, prices $(r, w)$ and an invariant probability measure $\Phi$ such that- Given prices $(r, w)$ and government policies $\left(\tau_{c}, \tau_{k}, T, \tau_{s s}, \bar{y}_{s s}\right)$, the value function $v$ satisfies the Bellman equation and ( $c, n, a^{\prime}$ ) are the associated policy functions.
- Given prices $(r, w)$, the optimal choices of the representative firm satisfy

$$
\begin{aligned}
r & =\Omega \epsilon \cdot\left[\frac{L}{K}\right]^{1-\epsilon}-\delta_{k} \\
w & =\Omega(1-\epsilon)\left[\frac{K}{L}\right]^{\epsilon} .
\end{aligned}
$$

- Government policies satisfy the government budget constraints.

Definition of Recursive Competitive Equilibrium (cont.)

- Market clearing:
- The labor market clears:

$$
L=\int e(j, s, \alpha, \eta) n(j, s, \alpha, \eta, a) d \Phi
$$

- The capital market clears

$$
(1+n)(K+B)=\int a^{\prime}(j, s, \alpha, \eta, a) d \Phi
$$

- The goods market clears

$$
Y=\int c(j, s, \alpha, \eta, a) d \Phi+(n+\delta) K+G
$$

- The invariant probability measure $\Phi$ is consistent with the population structure of the economy, with the exogenous processes $\pi_{s}$, and the household policy function $a^{\prime}($.$) .$


## Calibration of Initial Equilibrium: Overview

- Standard calibration for household demographics, preferences and technology parameters. Key parameters $(\gamma=1.5, \chi=0.6)$
- Exception: $e(j, s, \alpha, \eta)$ process. Want realistic earnings and wealth distribution.
- Goal: realistic earnings and wealth distribution
- Procedure to determine $w \cdot e(j, s, \alpha, \eta)$
- Choose aggregate TFP such that $w=1$
- Use $\varepsilon_{j, s}$ and $\alpha$ estimates from PSID
- Estimate baseline Markov chain $\left\{\eta_{s, 1}, \ldots, \eta_{s, 5}\right\}$ from PSID $\rightarrow$ normal labor earnings (roughly bottom 99\%)
- Augment with very high earnings realizations $\left\{\eta_{s, 6}, \eta_{s, 7}\right\}$
$\rightarrow$ follows Castaneda/Diaz-Jimenez/Rios-Rull (JPE, 2003)


## Calibration: High Earnings Realizations

No college education


College education


Ballpark numbers: If median income is $\$ 50,000$, average income of $\eta_{6}$ people is $\$ 450,000$, of $\eta_{7}$ people $\$ 20,000,000$ (population share $0.036 \%$ ).

## Exogenously Calibrated Parameters

| Parameter | Value/Target |
| :--- | ---: |
| Survival probabilities $\left\{\psi_{j}\right\}$ | HMD 2010 |
| Population growth rate $n$ | $1.1 \%$ |
| Capital share in production $\epsilon$ | $33 \%$ |
| Threshold positive taxation $\bar{y}_{l}$ | $35 \%$ of $y^{\text {med }}$ |
| Top tax bracket $\bar{y}_{h}$ | $400 \%$ of $\bar{y}$ |
| Top marginal tax rate $\tau_{h}$ | $39.6 \%$ |
| Consumption tax rate $\tau_{c}$ | $5 \%$ |
| Capital income tax $\tau_{k}$ | $28.3 \%$ |
| Government debt to GDP $B / Y$ | $60 \%$ |
| Government consumption to GDP $G / Y$ | $17 \%$ |
| Bend points $b_{1}, b_{2}$ | $0.184,1.114$ |
| Replacement rates $r_{1}, r_{2}, r_{3}$ | $90 \%, 32 \%, 15 \%$ |
| Pension Cap $\bar{y}_{s s}$ | $200 \%$ |
| Inverse of Frisch elasticity $\chi$ | 0.6 |

## Other Endogenously Calibrated Parameters

| Parameter | Value | Target/Data |
| :--- | ---: | :--- |
| Technology level $\Omega$ | 0.922 | $w=1$ |
| Depreciation rate $\delta_{k}$ | $7.6 \%$ | $r=4 \%$ |
| Initial marginal tax rate $\tau_{l}$ | $12.2 \%$ | Budget balance |
| Time discount factor $\beta$ | 0.977 | $K / Y=2.88$ |
| Disutility from labor $\lambda$ | 36 | $\bar{n}=33 \%$ |
| Coeff. of Relative Risk Aversion $\gamma$ | 1.5 | $\epsilon=0.25$ |

- Model-implied average tax elasticity of earnings in top $1 \%$ is $e=0.25$, same as assumed by Diamond and Saez (2011).


## Macroeconomic Aggregates in Benchmark Economy

| Variable | Value |
| :--- | ---: |
| Capital | $289 \%$ |
| Government debt | $60 \%$ |
| Consumption | $58 \%$ |
| Investment | $25 \%$ |
| Government Consumption | $17 \%$ |
| Av. hours worked (in \%) | $33 \%$ |
| Interest rate (in \%) | $4 \%$ |
| Tax revenues |  |
| $\quad$ - Consumption | $2.9 \%$ |
| - Labor | $11.9 \%$ |
| $\quad$ - Capital income | $4.0 \%$ |
| Pension System |  |
| Contribution rate (in \%) | $12.5 \%$ |
| Total pension payments | $5.1 \%$ |

## Earnings and Wealth Distribution

Model and Data

The Labor Earnings Distribution

|  | Quintiles |  |  |  |  |  | Top (\%) |  |  |  | Gini |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: |
|  | 1st | 2nd | 3rd | 4th | 5th | $90-95$ | $95-99$ | $99-100$ |  |  |  |
| Model | 0.0 | 5.6 | 10.9 | 17.2 | 66.3 | 10.9 | 18.9 | 22.8 | 0.649 |  |  |
| US Data | -0.1 | 4.2 | 11.7 | 20.8 | 63.5 | 11.7 | 16.6 | 18.7 | 0.636 |  |  |

The Wealth Distribution

|  | Quintiles |  |  |  |  |  | Top (\%) |  |  |  | Gini |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: |
|  | 1st | 2nd | 3rd | 4th | 5th | $90-95$ | $95-99$ | $99-100$ |  |  |  |
| Model | 0.0 | 0.9 | 4.2 | 11.5 | 83.4 | 14.1 | 25.3 | 30.6 | 0.809 |  |  |
| US Data | -0.2 | 1.1 | 4.5 | 11.2 | 83.4 | 11.1 | 26.7 | 33.6 | 0.816 |  |  |

## Thought Experiment: Tax Reform-Induced Transition

- Start from initial steady state with (crude approximation of) current US tax system and earnings and wealth distribution
- Unexpected one time change in tax policy
- Set $\bar{y}_{h}$ to the top $1 \%$ labor earnings threshold
- Change in top marginal tax rate $\tau_{h}$
- Reform $\left(\bar{y}_{h}, \tau_{h}\right)$ induces transition path to new long-run equilibrium
- Government budget balance:
- Set $\tau_{l}$ to balance intertemporal budget
- Sequence of government debt balances sequential budgets


## Thought Experiment: Tax Reform-Induced Transition



Initial equilibrium:

$$
\begin{array}{ll}
\bar{y}_{l}=0.35 \cdot y^{\mathrm{med}}, & \tau_{l}=11.1 \% \\
\bar{y}_{h}=4.0 \cdot y^{\text {aver }}, & \tau_{h}=39.6 \%
\end{array}
$$

## The Top 1\% Laffer curve



- Peak of NPV Laffer curve at $87 \%$.
- Policy reform reduces wealth at top drastically along transition.
- Labor supply at top even less elastic to $\tau_{h}$ in long run.


## Linking results to Diamond/Saez: Saez (2001) Formula

Revenue maximizing marginal tax rate above a threshold $y^{*}$

$$
\tau_{h}=\frac{1}{1+\underbrace{a \cdot \epsilon_{c}}_{\text {Subst. effect }}-\underbrace{\left(\epsilon_{c}-\epsilon_{u}\right)}_{\text {Inc. effect }}}
$$

In the model, at benchmark $\tau_{h}$ and peak $\tau_{h}$

- Pareto distribution parameter $a=1.80 \Rightarrow a=1.18$
- Average compensated tax rate elasticity $\epsilon_{c}=0.41 \Rightarrow \epsilon_{c}=0.43$
- Strong income effect $\epsilon_{c}-\epsilon_{u}=0.31 \Rightarrow \epsilon_{c}-\epsilon_{u}=0.32$
$\Rightarrow$ According to formula: Top $1 \%$ rate: $\tau_{h}=70 \%$ vs. peak $\tau_{h}=84 \%$


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- Strong income effect $\epsilon_{c}-\epsilon_{u}=0.31 \Rightarrow \epsilon_{c}-\epsilon_{u}=0.32$
$\Rightarrow$ According to formula: Top $1 \%$ rate: $\tau_{h}=70 \%$ vs. peak $\tau_{h}=84 \%$
Note: formula works well for right inputs. But $a, \epsilon_{c}, \epsilon_{u}$ not policy invariant


## The Welfare-Maximizing Top 1\% Tax Rate

Measuring Social Welfare

- Current generations

$$
v_{1}\left(j, s, \alpha, \eta, a+\Psi_{1}(j, s, \alpha, \eta, a)\right)=v_{0}(j, s, \alpha, \eta, a)
$$

- Future generations

$$
E v_{t}\left(1, s, \alpha, \bar{\eta},+\Psi_{t}\right)=E v_{0}(1, s, \alpha, \bar{\eta}, 0)
$$

- Total transfers

$$
W=\int \Psi_{1}(j, s, \alpha, \eta, a) d \Phi_{1}+\sum_{t=1}^{\infty}\left(\frac{1+n}{1+r_{0}}\right)^{t} \Psi_{t}
$$

- Optimal tax system minimizes $W$


## The Welfare-Maximizing Top 1\% Tax Rate

Measuring Social Welfare

- Fehr/Kindermann (2014) show that to a first order approximation (of the value function) this is equivalent to maximizing

$$
\begin{aligned}
W=\int \lambda(j, s, \alpha, \eta, a) \cdot v_{1} & (j, s, \alpha, \eta, a) d \Phi_{1} \\
& +\sum_{t=1}^{\infty}\left(\frac{1+n}{1+r_{0}}\right)^{t} \lambda_{t} \cdot E v_{t}(1, s, \alpha, \bar{\eta}, 0)
\end{aligned}
$$

with

$$
\begin{aligned}
\lambda(j, s, \alpha, \eta, a) & =U_{c}\left[c_{1}(j, s, \alpha, \eta, a), n_{1}(j, s, \alpha, \eta, a)\right]^{-1} \quad \text { and } \\
\lambda_{t} & =E\left[U_{c}\left[c_{t}(1, s, \alpha, \bar{\eta}, 0), n_{t}(1, s, \alpha, \bar{\eta}, 0)\right]\right]^{-1}
\end{aligned}
$$

## The Welfare-Maximizing Top 1\% Tax Rate



## Results: Transitional Dynamics



## Distribution of Welfare Gains



- Welfare gains for future cohorts: Ex ante redistribution or Ex post insurance? Mainly better ex post insurance!


## Results: Ex ante redistribution?



## Results: Ex ante redistribution?



- Why are the low skilled $(s=n) /$ high $\alpha$ so much better off?
- Why are the low skilled $(s=n) /$ low $\alpha$ only marginally better off?


## Results: Ex ante redistribution?

Mostly because

- Reduction in average tax rates is highest in the middle of the earnings distribution, not at the very bottom
- Aggregate wages fall substantially (in medium/long run)
- Also: lower skilled have the lower probability to climb up to the high income region


## Results: Ex ante redistribution?



## Better ex post insurance!




- For the bottom $99 \%$, mean consumption increases, variance of consumption declines, with tax reform ...
- ...despite the fact that aggregate consumption falls by $7 \%$.


## Better ex post insurance!

Total Population


Total Population


- Consumption of top $1 \%$ takes the entire hit.
- Matters for aggregate welfare, but not all that much.


## Sensitivity Analysis

- High Earnings Dispersion is Key for Optimal Tax Result
- Version of model without high earnings realizations (no $\eta_{6}, \eta_{7}$ ).
- Earnings and wealth distribution grossly counterfactual at top $1 \%$.
- Optimal top marginal tax rate approximately $35 \%$.
- Preferences $U(c, n)=\frac{c^{1-\gamma}}{1-\gamma}-\lambda \frac{n^{1+1 / \chi}}{1+1 / \chi}$
- Frisch elasticity $\chi$ has only moderate impact on the results
- Importance of size of income effect as parameterized by $\gamma$

| Variable | $\gamma=2$ | $\gamma=1.5$ |
| :--- | ---: | ---: |
| $e_{c}$ | 0.38 | 0.41 |
| $e_{u}$ | 0.01 | 0.10 |
| Peak Laffer NPV | $95 \%$ | $87 \%$ |
| Peak Laffer $t=\infty$ | $98 \%$ | $91 \%$ |
| Welfare Max | $89 \%$ | $79 \%$ |
| Welfare Max SS | $95 \%$ | $82 \%$ |

## To Sum Up...

- Life cycle general equilibrium model with realistic earnings and wealth inequality
- Peak of Laffer curve for top $1 \%$ earners at higher rates than projected by Diamond/Saez ( $\tau_{h}=87 \%$ )
- persistent and very high productivity shocks
- income effects important at the very top
- Very high marginal tax rate on top $1 \%$ labor earnings ( $\tau_{h}=79 \%$ ) is optimal in terms of aggregate welfare
- detrimental to macro aggregates
- but strong welfare gains from ex post insurance


## What is Next?

- Potentially (VERY?) problematic assumption 1: labor productivity process invariant to tax system
- human capital accumulation (Krueger and Ludwig 2016, Badel and Huggett 2016)
- entrepreneurial activity (Cagetti/de Nardi 2007, Brüggemann 2016)
- Potentially (VERY?) problematic assumption 2: Closed economy? How elastic are the location decisions of the "super stars"?
(Akcigit, Baslandze and Stantcheva 2016)
- Administrative data can give quantitatively crucial insights into
- who the top $1 \%$ actually are and
- how long they stay up there.


## THANK YOU FOR COMING AND LISTENING!

## Sensitivity Analysis

| Variable | $\gamma=2.0$ | $\gamma=1.5$ | $\gamma=1.0$ |
| :--- | ---: | ---: | ---: |
| $e_{c}$ | 0.38 | 0.41 | 0.46 |
| $e_{u}$ | 0.01 | 0.10 | 0.22 |
| Peak Laffer NPV | $95 \%$ | $87 \%$ | $79 \%$ |
| Peak Laffer $t=\infty$ | $98 \%$ | $91 \%$ | $84 \%$ |
| Welfare Max | $89 \%$ | $79 \%$ | $64 \%$ |
| Welfare Max SS | $95 \%$ | $82 \%$ | $69 \%$ |

- Not only peak of Laffer curve at lower rate, also lesser additional revenues from increasing $\tau_{h}$


## Calibration of initial equilibrium

Wage process

- The baseline wage process

$$
\log e(j, s, \alpha, \eta)=\alpha_{s}+\varepsilon_{j, s}+\eta_{j, s}
$$

with

$$
\eta_{j, s}=\rho_{s} \eta_{j-1, s}+\nu_{j, s} \quad \nu_{j, s} \sim N\left(0, \sigma_{\nu, s}^{2}\right)
$$

- Estimates from PSID

|  | $\rho_{s}$ | $\sigma_{\nu}^{2}$ | $\sigma_{\alpha}^{2}$ | $\phi_{s}$ |
| :---: | :---: | :---: | :---: | :---: |
| $s=n$ | 0.9850 | 0.0346 | 0.2061 | 0.59 |
| $s=c$ | 0.9850 | 0.0180 | 0.1517 | 0.41 |

## Results

Transitional Dynamics: Macroeconomic Aggregates



## Results

## Transitional Dynamics: Hours and Tax Revenues




## Results

Transitional Dynamics: Wages, Interest Rates



## More on the Formula

- Diamond/Saez (2011): Revenue maximizing top marginal tax rate:

$$
\tau_{h}=\frac{1}{1+a \cdot e}
$$

- Why might the formula potentially be wrong/misleading/not useful?
(1) $a, e$ are not constants, but depend on policy: $a\left(\tau_{h}\right), e\left(\tau_{h}\right)$. Fixed point problem!
(2) Formula only applies to very specific tax experiment that leaves remainder of tax code completely unchanged.
(3) It does not apply to dynamic general equilibrium models.
- Note: Badel and Huggett (2016) develop generalized formula that tackles problem 3 (but not items 1 and 2).


## Related Literature (selective and likely incomplete)

- Empirical motivation: top income shares and taxes: Piketty and Saez (2003, 2011), Alvavedo et al. (2013), Akcigit, Baslandze and Stantcheva (2016)
- Static optimal tax literature: Mirrlees (1971), Diamond (1998), Saez (2001), Piketty, Saez and Stantcheva (2014); Diamond and Saez (2011)
- Laffer curve and tax progressivity in dynamic quantitative macro models: Trabandt and Uhlig (2011), Fehr and Kindermann, Holter et al. (2016), Guner et al. (2016), Badel and Huggett (2016)
- Optimal Progressive Income Taxation: Conesa and Krueger (2006), Bruggemann (2016)


## More on the Top 1\%

- Household income of 389,436 in 2013 to make it into Top $1 \%$
- Top $1 \%$ earned $19 \%$ of all AGI, paid $35 \%$ of federal income taxes.
- Having (reporting?) top incomes is transitory: between 1999 and 2007, of those reporting income of 1 Mill. or more
- Only $50 \%$ did so for one year
- $2 / 3$ did so for one or two year
- Only approx. $10 \%$ for all years
- What do they do (Bakija et al.2012)? Of top $0.1 \%$ income earners:
- $60 \%$ executives, managers, supervisors, and financial professionals
- Small but important minority at the very top are sports/entertainment stars and entrepreneurs
- Almost $50 \%$ of earned income of this group from pass-through entities (sole proprietorships, partnerships, S-corps)


## More on the Top $1 \%$ in the Model

- $\eta_{7}$ shock is large, persistent, but strongly mean reverting.
- Relative to model with permanently high productivity (or static model), superstars (for given level of wealth):
- Work more (and respond less to increases in marginal tax rate)
- Save more and consume less


## Policy Functions of Superstars

Our Model vs. Permanent Superstars: Hours and Asset Accumulation



## Labor Supply Elasticity to Tax Changes of Superstars, Decomposition of Laffer Curve




## Why Dynamics, Why Transition?

- Value of Dynamic Model
- Importance of wealth accumulation for labor supply response, especially of high $\eta$ individuals.
- Laffer curve very different in long run since wealth distribution shifts to the left.
- Factor price response qualitatively different than in static model ( $w$ down rather than up).
- Importance of Transitional Dynamics
- For $t=1$ Laffer curve similar to that static model. Steady state overstates revenue maximizing $\tau_{h}$.
- Factor price response differs in short run ( $w$ up), long run ( $w$ down).
- Importance of transitional generations in social welfare. Steady state overstates welfare maximizing $\tau_{h}$.


## Comparison of Static and Dynamic Model

static
dynamic

|  | GE | no | no | no | no |  | no | no | yes | yes |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Wealth | no | no | no | yes |  | yes | yes | yes | yes |  |
| $\gamma$ | 0.00 | 0.78 | 0.78 | 0.87 |  | 1.50 | 1.50 | 1.50 | 1.50 |  |
|  |  |  |  |  |  | $t=1$ | $t=\infty$ | $t=1$ | $t=\infty$ |  |
| $a_{0}$ | 2.14 | 1.77 | 1.77 | 1.68 |  | 1.80 | 1.80 | 1.80 | 1.80 |  |
| $e_{c}$ | 0.24 | 0.41 | 0.41 | 0.42 |  | 0.41 | 0.33 | 0.41 | 0.33 |  |
| $e_{u}$ | 0.24 | 0.11 | 0.11 | 0.12 |  | 0.10 | -0.12 | 0.10 | -0.12 |  |
| $e_{0}$ | 0.24 | 0.24 | 0.24 | 0.24 |  | 0.24 | 0.08 | 0.24 | 0.08 |  |
| $\tau_{0}^{\mathrm{LF}}$ | 0.66 | 0.70 | 0.70 | 0.71 |  | 0.70 | 0.87 | 0.70 | 0.87 |  |
| $a$ | 1.35 | 1.04 | 1.04 | 1.14 |  | 1.33 | 1.04 | 1.30 | 1.05 |  |
| $e_{c}$ | 0.24 | 0.40 | 0.40 | 0.42 |  | 0.46 | 0.41 | 0.46 | 0.39 |  |
| $e_{u}$ | 0.24 | 0.13 | 0.10 | 0.17 |  | 0.22 | 0.03 | 0.22 | -0.01 |  |
| $e$ | 0.24 | 0.14 | 0.11 | 0.20 |  | 0.28 | 0.05 | 0.28 | 0.01 |  |
| $\tau^{\text {LF }}$ | 0.76 | 0.87 | 0.89 | 0.81 |  | 0.73 | 0.95 | 0.73 | 0.99 |  |
| $\tau_{\text {sim }}^{\text {LF }}$ | 0.76 | 0.87 | 0.85 | 0.82 |  | 0.78 | 0.94 | 0.80 | 0.91 |  |

