

Due by Wednesday, February 8, 2023 at 11:59pm onQ

#1. Consider the following **first-price, sealed-bid private value auction**. There are 5 bidders. Each bidder's valuation (v_i for bidder i) for the object follows the standard uniform distribution $U[0,1]$. These valuations are distributed independently. Suppose that the seller sets a minimum price (i.e., reserve price) r . Find the symmetric Bayesian equilibrium bidding function $b_i = B(v_i)$ in this auction.

#2. Consider the following two-player simultaneous-move game played repeatedly with discount factor δ .

(a) If this game is played two times. Find all subgame perfect equilibria in that game.

(b) Now suppose it is played infinitely many times. In a figure, identify the players' payoffs which can be sustained as the average per-period payoffs in a subgame perfect equilibrium when δ approaches 1.

| | C | D |
|-----|------|------|
| A | 1, 2 | 0, 0 |
| B | 2, 1 | 3, 2 |

#3. Consider the following simultaneous-move game played infinitely many times between two players. Draw the area for the feasible and individually rational payoffs for the two players in a figure.

| | C | D |
|-----|------|------|
| A | 1, 2 | 3, 0 |
| B | 2, 1 | 1, 0 |

#4. Consider the following 2-player simultaneous-move game with asymmetric information. Player 1 knows which game they are playing. Player 2 only knows that with probability q , game (1) is played; with probability $1 - q$, game (2) is played. Find all pure-strategy Bayesian equilibria in this game.

game (1)

| | C | D |
|-----|------|------|
| A | 1, 1 | 1, 3 |
| B | 2, 4 | 2, 2 |

game (2)

| | C | D |
|-----|------|------|
| A | 2, 1 | 2, 3 |
| B | 1, 4 | 1, 2 |